

I. Решите операционным методом следующее линейное неоднородное дифференциальное уравнение:

- 1)  $y'' - 2y' + y = \sin t, \quad y(0) = 0, y'(0) = 1$
- 2)  $y''' - y' = t, \quad y(0) = y'(0) = 0, y''(0) = 1$
- 3)  $y'' + 2y' + 5y = 1, \quad y(0) = 1, y'(0) = 0$
- 4)  $y''' + y' = 2, \quad y(0) = y''(0) = 0, y'(0) = 1$
- 5)  $y'' + y' = \cos t, \quad y(0) = 0, y'(0) = 1$
- 6)  $y'' + 4y' = \sin t, \quad y(0) = 0, y'(0) = 1$
- 7)  $y'' - 4y' = t - 1, \quad y(0) = 1, y'(0) = -1$
- 8)  $y'' - y = \sin t, \quad y(0) = 0, y'(0) = 1$
- 9)  $y'' + y = t, \quad y(0) = 1, y'(0) = 2$
- 10)  $y'' - 5y' + 6y = e^{-t}, \quad y(0) = 0, y'(0) = 1$
- 11)  $y'' + y = 3t + 1, \quad y(0) = 0, y'(0) = 1$
- 12)  $y'' - y = -t^2 - 2t, \quad y(0) = 0, y'(0) = 2$
- 13)  $y'' - 4y' = 8t - 2, \quad y(0) = 5, y'(0) = 4$
- 14)  $y'' + y = 3 - 2t, \quad y(0) = 4, y'(0) = -1$
- 15)  $y'' - y' = -2, \quad y(0) = 0, y'(0) = 1$
- 16)  $y'' - y' - 2y = e^t, \quad y(0) = 0, y'(0) = 0,25$
- 17)  $y'' - 4y' + 3y = e^{2t}, \quad y(0) = 0, y'(0) = 3$

II. Найдите решение задачи Коши для системы дифференциальных уравнений операционным методом:

- 1)  $\begin{cases} x' = x - 2y \\ y' = x - y \end{cases}, \quad x(0) = 1, y(0) = 0$
- 2)  $\begin{cases} x' = x + y \\ y' = 8x + 3y \end{cases}, \quad x(0) = 0, y(0) = 2$
- 3)  $\begin{cases} x' = x - 4y \\ y' = x + y \end{cases}, \quad x(0) = 0, y(0) = 1$
- 4)  $\begin{cases} x' = x + y \\ y' = -x - y \end{cases}, \quad x(0) = -2, y(0) = 1$
- 5)  $\begin{cases} x' = 2x - y \\ y' = x + 4y \end{cases}, \quad x(0) = 1, y(0) = 0$
- 6)  $\begin{cases} x' = -x + y \\ y' = -2x + y \end{cases}, \quad x(0) = 0, y(0) = 1$
- 7)  $\begin{cases} x' = 3x + y \\ y' = -x + y \end{cases}, \quad x(0) = 3, y(0) = 0$
- 8)  $\begin{cases} x' = 3x + y \\ y' = -x + 5y \end{cases}, \quad x(0) = 0, y(0) = 2$
- 9)  $\begin{cases} x' = 5x - y \\ y' = x + 3y \end{cases}, \quad x(0) = 1, y(0) = 0$

- 10)  $\begin{cases} x' = 12x - 5y \\ y' = 5x + 12y \end{cases}, \quad x(0) = 1, y(0) = 1$
- 11)  $\begin{cases} x' = x - y \\ y' = 4x - 3y \end{cases}, \quad x(0) = 3, y(0) = 0$
- 12)  $\begin{cases} x' = -x - 10y \\ y' = 2x + 3y \end{cases}, \quad x(0) = 7, y(0) = -1$
- 13)  $\begin{cases} x' = 3x - y \\ y' = x + 5y \end{cases}, \quad x(0) = 2, y(0) = 0$
- 14)  $\begin{cases} x' = -2x - 5y \\ y' = x \end{cases}, \quad x(0) = 7, y(0) = -1$
- 15)  $\begin{cases} x' = x - 2y \\ y' = 2x - 3y \end{cases}, \quad x(0) = 0, y(0) = 1$
- 16)  $\begin{cases} x' = x + y \\ y' = -4x + y \end{cases}, \quad x(0) = 1, y(0) = 2$
- 17)  $\begin{cases} x' = -3x + 4y \\ y' = -x + y \end{cases}, \quad x(0) = 0, y(0) = 3$